

KARABUK UNIVERSITY, ENGINEERING FACULTY, AUTOMOTIVE ENGINEERING, FLUID MECHANICS, MIDTERM EXAM, 20.11.2012

**Attention: Forbidden to use extra paper. You can use the blank space on the page. Everyone's questions and options are different from others. Time is 45 minutes. The draft solutions on the page will not read. Only will looked the options. If you think there is a mistake in the questions, tick to the nearest answer. Then it will be evaluated in your benefit to. You can use the back of page as a draft. I wish you success... Asist.Prof.Dr.İbrahim Çayıröglü**

@Question-1: As shown in the figure, the pressure in the tube  $P=25000\text{Pa}$ .  $d_1$  (density)= $975\text{kg/m}^3$ ,  $d_2$  (density)= $950\text{kg/m}^3$ ,  $h_1=0,5\text{m}$ ,  $h_2=0,25\text{m}$ ,  $A$  (area) = $0,025\text{m}^2$ . Accordingly, What is the  $F$  force as Newton?  
 ©480,418 ©549,05 ©617,681 ©686,312 ©960,837 ©1029,468 ©1098,099 ©1166,73 ©1235,362 ©1303,993 ©1372,624 ©.....

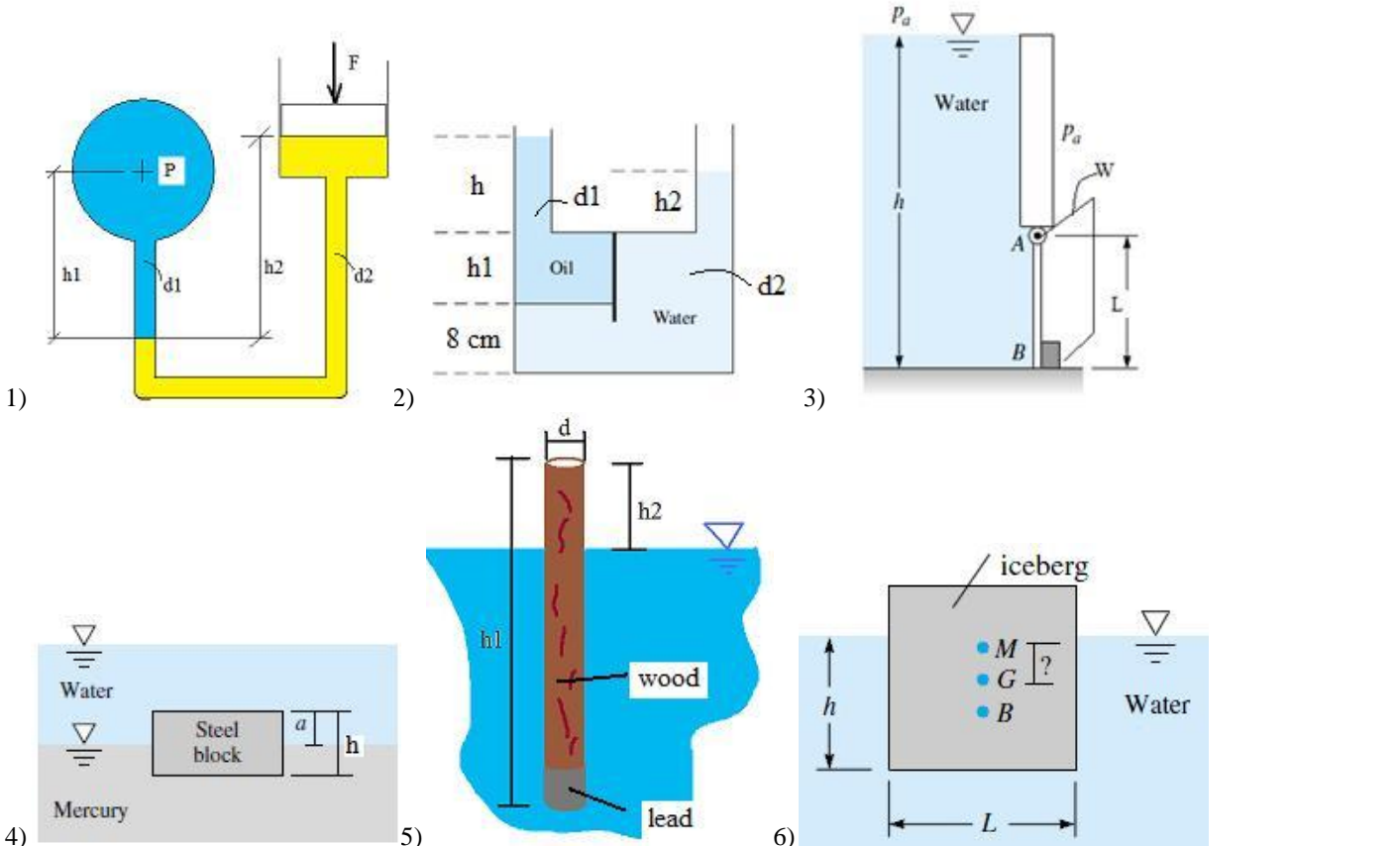
@Question-2: In Figure the tank contains water and immiscible oil at  $20^\circ\text{C}$ . What is  $h$  in meter if the density of the oil is  $=875\text{kg/m}^3$  ? The density of water (you must be know).  $h_1=0,5\text{m}$ .  $h_2=0,25\text{m}$ .  
 ©0,107 ©0,143 ©0,178 ©0,214 ©0,25 ©0,286 ©0,321 ©0,357 ©0,643 ©0,678 ©0,714 ©.....

@Question-3: Gate AB in Figure is  $W=5\text{m}$  wide into the paper, hinged at A, and restrained by a stop at B. The water is at  $20^\circ\text{C}$  compute the force (N) on stop B if the water depth  $h=25\text{m}$ . and  $L=8,33\text{m}$ .  
 ©4256449,864 ©4682094,85 ©5107739,837 ©5533384,823 ©5959029,81 ©6384674,796 ©6810319,782 ©7235964,769 ©7661609,755 ©8087254,742 ©8512899,728 ©.....

@Question-4: A uniform block of steel (density= $7,6$ ) will float at a mercury-water interface as in Figure. What is the distance  $a$  for this condition  $h=25\text{cm}$ ? (mercury density= $13,81$ )  
 ©12,119 ©13,331 ©14,543 ©15,755 ©16,967 ©18,178 ©19,39 ©20,602 ©21,814 ©23,026 ©24,238 ©.....

@Question-5: As shown in the figure we make a pycnometer from wood which density =  $0,5$  diameter  $d=2,5\text{ cm}$  and height  $h_1=25\text{ cm}$  . When we put it into water, we want to  $h_2=6,25\text{ cm}$ . Accordingly what is the amount of the Lead as kg ? (Lead density= $11,25$ )  
 ©0,029 ©0,032 ©0,038 ©0,042 ©0,045 ©0,048 ©0,051 ©0,054 ©0,058 ©0,061 ©0,064 ©.....

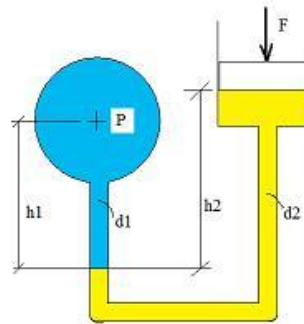
@Question-6: An iceberg can be idealized as a cube of side length  $L=25\text{m}$ , as in Figure. If seawater is denoted by  $d_1=1,025$ , then glacier ice (which forms icebergs) has  $d_2=0,75$ . Determine the MG distance for this 'cubic' iceberg is stable or not for the position shown in figure.  
 ©-0,455 ©-0,506 ©-0,607 ©-0,658 ©-0,708 ©-0,759 ©-0,81 ©-0,86 ©-0,911 ©-0,961 ©-1,012 ©.....



## ANSWERS

1) As shown in the figure, the pressure in the tube  $P=25000\text{Pa}$ .  $d_1$  (density)= $975\text{kg/m}^3$ ,  $d_2$  (density)= $950\text{kg/m}^3$ ,  $h_1=0,5\text{m}$ ,  $h_2=0,25\text{m}$ ,  $A$  (area) = $0,025\text{m}^2$ . Accordingly, What is the  $F$  force as Newton?

$P=25000\text{ Pa}$   
 $d_1 = 975\text{kg/m}^3$  (density)  
 $d_2 = 950\text{kg/m}^3$   
 $h_1=0,5\text{m}$ ,  
 $h_2=0,25\text{m}$   
 $A = 0,025\text{m}^2$   
 $F=?$



$$P + (d_1 * 9.81 * h_1) - (d_2 * 9.81 * h_2) - F/A = 0$$

$$F = A * (P + (d_1 * 9.81 * h_1) - (d_2 * 9.81 * h_2))$$

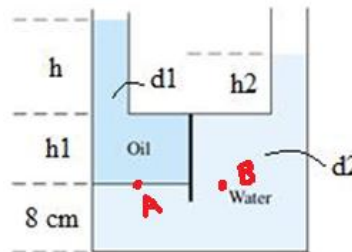
$$F = 0.025 * (25000 + (975 * 9.81 * 0.5) - (950 * 9.81 * 0.25))$$

$$F = 0.025 * (25000 + (4782,37) - (2329,87))$$

$$F = \underline{686,31\text{ N}}$$

2) In Figure the tank contains water and immiscible oil at  $20^\circ\text{C}$ . What is  $h$  in meter if the density of the oil is  $=875\text{kg/m}^3$  ? The density of water (you must be know).  $h_1=0,5\text{m}$ .  $h_2=0,25\text{m}$ .

$d_1 = 875\text{kg/m}^3$   
 $h_1 = 0,5\text{m}$   
 $h_2 = 0,25\text{m}$   
 $d_2 = 1000\text{ kg/m}^3$   
 $h=?$



$$P_A = P_B$$

$$d_1 * g * (h + h_1) = d_2 * g * (h_1 + h_2)$$

$$d_1 * h + d_1 * h_1 = d_2 * (h_1 + h_2)$$

$$h = (d_2 * (h_1 + h_2) - d_1 * h_1) / d_1$$

$$h = (1000 * (0,5 + 0,25) - 875 * 0,5) / 875$$

$$h = (750 - 437,5) / 875$$

$$h = \underline{0,357\text{ m}}$$

3) Gate AB in Figure is  $W= 5\text{m}$  wide into the paper, hinged at A, and restrained by a stop at B. The water is at  $20\text{ C}$  compute the force (N) on stop B if the water depth  $h= 25\text{m}$ . and  $L = 8,33\text{m}$ .

$W= 5\text{m}$   
 $L = 8,33\text{m}$ ;  
 $h= 25\text{m}$

$$P_G = d * g * (h - L/2)$$

$$P_G = 1000 * 9.81 * (25 - 8,33/2)$$

$$P_G = 1000 * 9.81 * (20,83)$$

$$P_G = 204391,35\text{ Pa}$$

$$F = P_G * A$$

$$F = P_G * (L * W)$$

$$F = 204391,35 (8,33 * 5)$$

$$F = 8512899,72\text{ N}$$

$$e = \frac{I_G}{z_G A}$$

$$e = (w * L^3 / 12) / [(h - L/2) * (L * W)]$$

$$e = (5 * 8,33^3 / 12) / [(25 - 8,33/2) * (8,33 * 5)]$$

$$e = (240,83) / [(20,83) * (41,65)]$$

$$e = (240,83) / [867,56]$$

$$e = 0,277\text{ m}$$

$$F * (L/2 + e) = F_B * L$$

$$F_B = [F * (L/2 + e)] / L$$

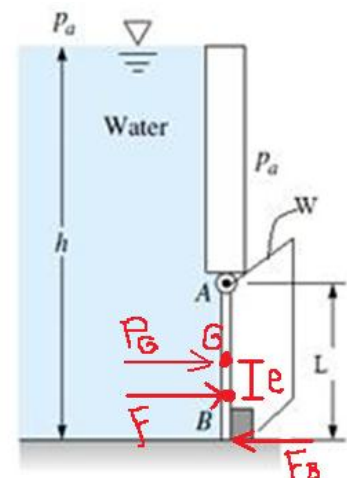
$$F_B = [8512899,72 * (8,33/2 + 0,277)] / 8,33$$

$$F_B = [8512899,72 * (4,442)] / 8,33$$

$$F_B = [37814300,55] / 8,33$$

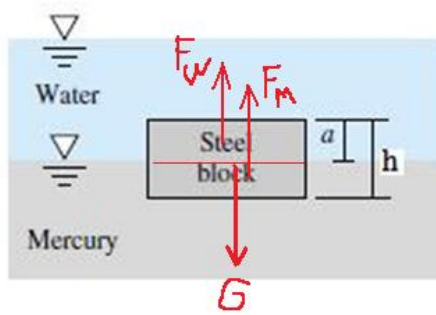
$$F_B = \underline{4\,539\,531,87\text{ N}}$$

There is no answer in options. Therefore, the answer had to be written in extra option.



4) A uniform block of steel (density= 7,6) will float at a mercury-water interface as in Figure. What is the distance a for this condition h=25cm? (mercury density=13,81)

$d_1 = 7,6 * 1000 \text{ kg/m}^3$   
 $d_2 = 13,81 * 1000 \text{ kg/m}^3$   
 $d_3 = 1 * 1000 \text{ kg/m}^3$   
 $h = 25 \text{ cm}$   
 $a = ?$



$G = d_1 * g * (L * W * h)$   
 $F_w = d_3 * g * (L * W * a)$   
 $F_m = d_2 * g * (L * W * (h-a))$

$G = F_w + F_m$   
 $d_1 * g * (L * W * h) = d_3 * g * (L * W * a) + d_2 * g * (L * W * (h-a))$   
 $d_1 * h = d_3 * a + d_2 * (h-a)$   
 $d_1 * h = d_3 * a + d_2 * h - d_2 * a$   
 $d_1 * h = a(d_3 - d_2) + d_2 * h$   
 $(d_1 * h) - (d_2 * h) = a(d_3 - d_2)$

$a = ((d_1 * h) - (d_2 * h)) / (d_3 - d_2)$   
 $a = ((7600 * 0,25) - (13810 * 0,25)) / (1000 - 13810)$  (Note: We can use relative density here, Then it would be much simpler)  
 $a = ((1900) - (3452,5)) / (-12810)$   
 $a = (-1552,5) / (-12810) = 0,121 \text{ m}$   
 $a = \underline{0,121 \text{ m}} = 12,1 \text{ cm}$

5) As shown in the figure we make a pycnometer from wood which density = 0,5 diameter d=2,5 cm and height h1=25 cm . When we put it into water, we want to h2 =6,25 cm. Accordingly what is the amount of the Lead as kg ? (Lead density=11,25)

$d = 2,5 \text{ cm}$  // diameter of the wood  
 $h_1 = 25 \text{ cm}$   
 $h_2 = 6,25 \text{ cm}$   
 $d_1 = 0,5$  // wood density  
 $d_2 = 11,25$  //lead density

//converted to meters.  
 $d = d / 100 = 0,025 \text{ m}$   
 $h_1 = h_1 / 100 = 0,25 \text{ m}$   
 $h_2 = h_2 / 100 = 0,0625 \text{ m}$

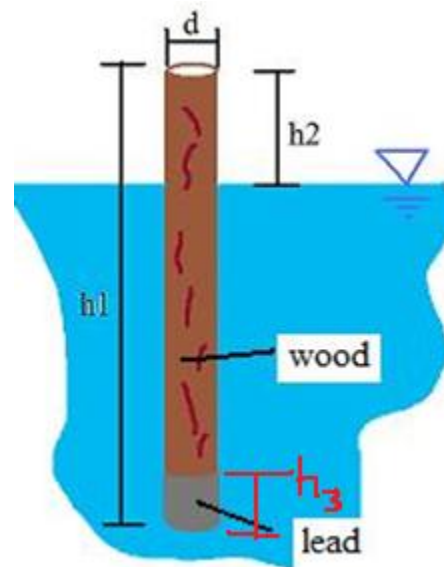
$area = 3.14 * (d / 2)^2 = 0,000499625 \text{ m}^2$   
 $V_{submerged} = area * (h_1 - h_2)$   
 $V_{submerged} = 0,000499625 * (0,25 - 0,0625) = 0,00009199 \text{ m}^3$

$F_{buoyancy} = 1000 * 9.81 * V_{submerged}$   
 $F_{buoyancy} = 1000 * 9.81 * 0,00009199$   
 $F_{buoyancy} = 0,90244 \text{ N}$

$weight = F_{buoyancy}$   
 $weight = 0,90244 \text{ N}$

$AverageDensity = mass / volume \Rightarrow mass = weight/g \Rightarrow mass = 0,90244 / 9,81 = 0,0919921 \text{ kg.}$   
 $AverageDensity = mass / (3.14 * r^2 * h_1)$   
 $AverageDensity = 0,0919921 / (3.14 * 0,0125^2 * 0,25)$   
 $AverageDensity = 750 \text{ kg/m}^3 \Rightarrow as \text{ relatif} = 0,75$

$ObjectMass = WoodMass + LeadMass$   
 $AverageDensity * ObjectVolume = WoodDensity * WoodVolume + LeadDensity * LeadVolume$   
 $0,750 * (area * h_1) = 0,500 * (area * (h_1 - h_3)) + 11,250 * (area * h_3)$   
 $0,750 * h_1 = 0,500 * (h_1 - h_3) + 11,250 * h_3$   
 $0,750 * h_1 = 0,500 * h_1 - 0,500 h_3 + 11,250 * h_3$   
 $0,750 * h_1 - 0,500 * h_1 = 10,75 * h_3$   
 $h_3 = (0,750 * h_1 - 0,500 * h_1) / 10,75$



$$h_3 = (0,750 * 0,25 - 0,500 * 0,25) / 10,75$$

$$h_3 = 0,005813 \text{ m}$$

$$\text{LeadMass} = V_{\text{kursun}} * d_2 * 1000$$

$$\text{LeadMass} = \text{Alan} * h_3 * d_2 * 1000$$

$$\text{LeadMass} = 0,000499625 * 0,005813 * 11,25 * 1000$$

$$\text{LeadMass} = \mathbf{0,03267 \text{ kg} = 32,67 \text{ gr}}$$

6) An iceberg can be idealized as a cube of side length  $L = 25\text{m}$ , as in Figure. If seawater is denoted by  $d_1 = 1,025$ , then glacier ice (which forms icebergs) has  $d_2 = 0,75$ . Determine the MG distance for this 'cubic' iceberg is stable or not for the position shown in figure.

$$L = \text{CubeEdge} = 25\text{m}$$

$$d_1 = \text{WaterDensity} = 1,025$$

$$d_2 = \text{IcebergDensity} = 0,75$$

$$F_{\text{buoyancy}} = G_{\text{iceberg}}$$

$$H_{\text{submerged}} * \text{WaterDensity} = \text{IcebergDensity} * \text{CubeEdge}^3$$

$$H_{\text{submerged}} = \text{IcebergDensity} * \text{CubeEdge}^3 / \text{WaterDensity}$$

$$h = d_2 * L^3 / d_1$$

$$h = 0,75 * 25^3 / 1,025$$

$$h = 18,292 \text{ m}$$

$$B_{\text{Adistance}} = h / 2 = 9,146 \text{ m}$$

$$G_{\text{Adistance}} = L / 2 = 12,5 \text{ m}$$

$$I = \text{MomentofInertia} = L * L^3 / 12$$

$$I = 25^4 / 12 = 32552 \text{ m}^4$$

$$\text{VolumeSubmerged} = L * L * h$$

$$\text{VolumeSubmerged} = 25 * 25 * 18,292$$

$$\text{VolumeSubmerged} = 11432,5 \text{ m}^3$$

$$M_{B\text{distance}} = I / \text{VolumeSubmerged}$$

$$M_{B\text{distance}} = 32552 / 11432,5$$

$$M_{B\text{distance}} = 2,847 \text{ m}$$

$$G_{B\text{distance}} = G_{\text{Adistance}} - B_{\text{Adistance}}$$

$$G_{B\text{distance}} = 12,5 - 9,146 = 3,354 \text{ m}$$

$$M_{G\text{distance}} = M_{B\text{distance}} - G_{B\text{distance}}$$

$$M_{G\text{distance}} = 2,847 - 3,354$$

$$M_{G\text{distance}} = \mathbf{-0,507 \text{ m} \quad \text{the iceberg tilt over}}$$

