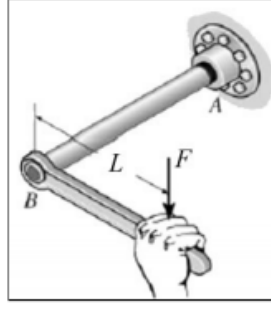
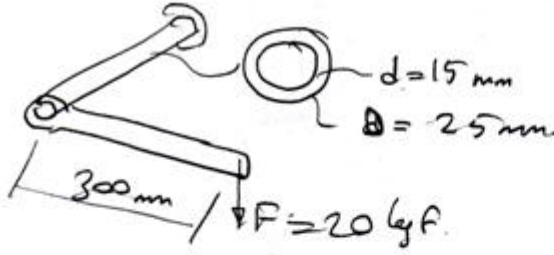


ÇÖZÜMLER

Soru-1(20p.) Şekildeki AB borusunun iç çapı 15 mm, dış çapı 25 mm dir. Kişi eliyle boruya 300 mm boyundaki anahtarla 20 kgf uygularsa boruda oluşacak en büyük Burulma Kayma gerilmesi kaç MPa olur? (birimlere dikkat edin!) ©4,19011 ©6,1749 ©8,15969 ©11,46767 ©13,23192 ©15,87831 ©18,08363 ©18,08363 ©22,0532 ©23,59693 ©24,69959 ©28,00757 ©26,46384 ©27,5665 ©31,31555 ©29,77182 ©.....



①



$$F = 20 \text{ kgf} \cdot 9,81 = 196,2 \text{ N}$$

$$M_b = F \cdot L = 196,2 \text{ N} \cdot 300 \text{ mm} = 58860 \text{ Nmm}$$

$$\tau_b = \frac{M_b}{I_p/r} = \frac{58860 \text{ Nmm}}{\frac{33379 \text{ mm}^4}{12,5 \text{ mm}}}$$

$$I_p = \frac{\pi}{32} (D^4 - d^4) = \frac{\pi}{32} (25^4 - 15^4)$$

$$\tau_b = \underline{22,042 \text{ MPa}}$$

$$I_p = 33379 \text{ mm}^4$$

$$r = \frac{D}{2} = \frac{25 \text{ mm}}{2} = 12,5 \text{ mm}$$

Soru-2(20p.) Şekildeki gibi bir kiriş iki noktadan mesnetlenmiş ve iki noktadan üzerine kuvvet uygulanmıştır. Verilen ölçülere göre kirişte meydana gelecek en büyük eğilme gerilmesi ne olur?

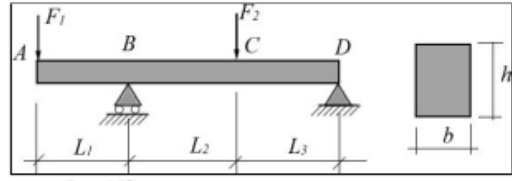
($F_1=1000\text{ N}$, $F_2=2000\text{ N}$, $L_1=500\text{ mm}$, $L_2=L_3=800\text{ mm}$, $b=30\text{ mm}$, $h=40\text{ mm}$) ©35,0625

©35,75 ©48,125 ©46,75 ©54,3125 ©61,875

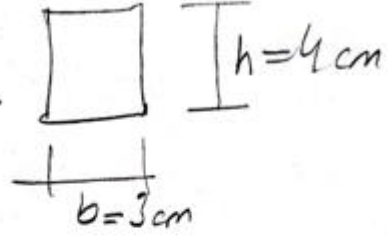
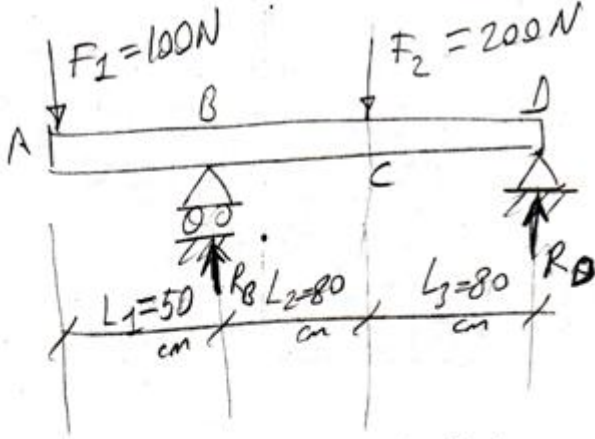
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©89,375 ©93,5 ©107,25 ©101,75 ©99,6875

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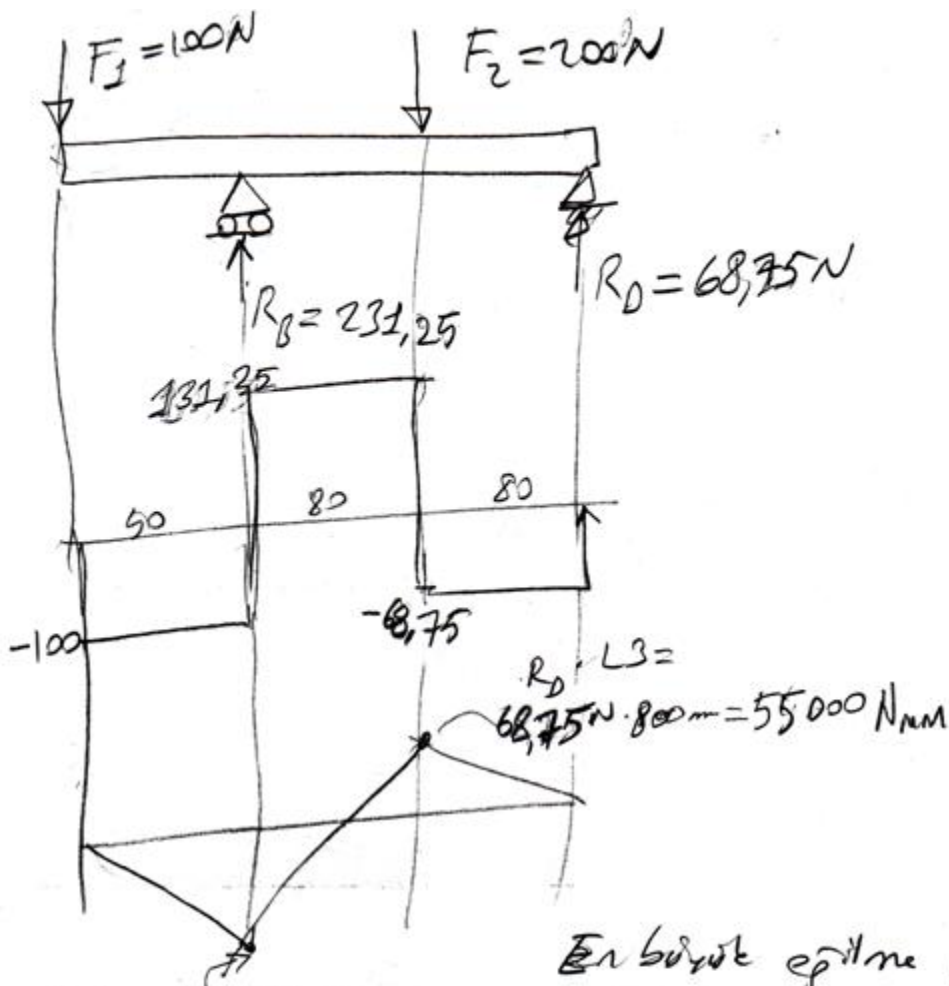
②



Önce mesnet kuvvetlerini bulalım.

$$\begin{aligned} \sum M_B = 0 & \quad -F_1 \cdot L_1 + F_2 \cdot L_2 - R_D \cdot (L_2 + L_3) = 0 \\ -1000 \cdot 500 + 2000 \cdot 800 - R_D (1600) & = 0 \\ R_D = \frac{160000 - 500000}{1600} = \frac{-340000}{1600} & = -212,5 \text{ N} \end{aligned}$$

$$\begin{aligned} \sum M_D = 0 & \quad -F_1 (L_1 + L_2 + L_3) + R_B (L_2 + L_3) - F_2 (L_3) = 0 \\ -1000 (500 + 800 + 800) + R_B (800 + 800) - 2000 (800) & = 0 \\ -210000 \text{ Nmm} + R_B \cdot 1600 \text{ mm} - 1600000 \text{ Nmm} & = 0 \\ R_B = \frac{370000 \text{ Nmm}}{1600 \text{ mm}} = 231,25 \text{ N} \end{aligned}$$



$$F_2 \cdot L_2 = 100 \text{ N} \cdot 50 \text{ mm} = 5000 \text{ Nmm}$$

Erhöhte epiline Momente,

$$M_e = 55,000 \text{ Nmm}$$

$$\sigma_e = \frac{M_e}{I/c}$$

$$I_x = \frac{bh^3}{12} = \frac{30 \text{ mm} \cdot 40 \text{ mm}^3}{12}$$

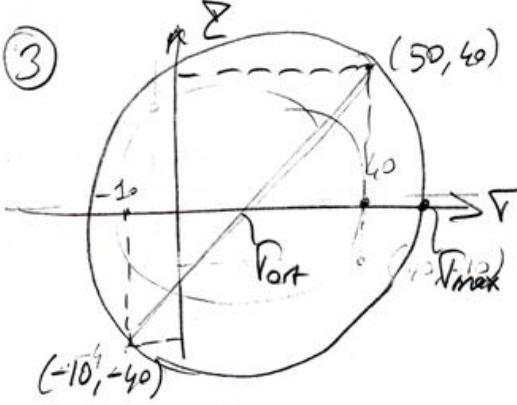
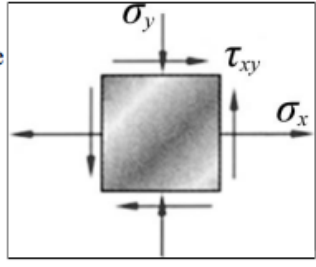
$$I_x = 160.000 \text{ mm}^4$$

$$\sigma_e = \frac{55000 \text{ Nmm}}{\frac{160000 \text{ mm}^4}{20 \text{ mm}}}$$

$$c = \frac{h}{2} = \frac{40 \text{ mm}}{2} = 20 \text{ mm}$$

$$\sigma_e = 6,875 \text{ MPa} \left[\frac{\text{N}}{\text{mm}^2} \right]$$

Soru-3)(20p.) Bir malzemenin üzerinden alınan küçük bir parçanın üzerinde oluşan gerilmeler x ve y yönlerinde şekilde gibi olmaktadır. Bu malzemede meydana gelen en büyük Normal gerilme nedir? ($\sigma_x = 50 \text{ MPa}$, $\sigma_y = -10 \text{ MPa}$, $\tau_{xy} = \pm 40 \text{ MPa}$)
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$$\sigma_{ort} = \frac{\sigma_x + \sigma_y}{2}$$

$$= \frac{50 + (-10)}{2}$$

$$\sigma_{ort} = 20 \text{ MPa}$$

$$R = \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$$

$$R = \sqrt{\left(\frac{50 - (-10)}{2}\right)^2 + 40^2}$$

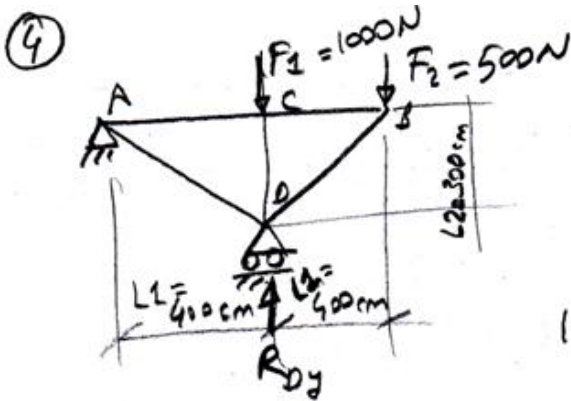
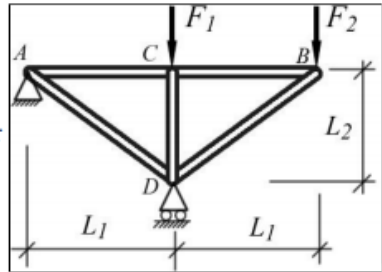
$$R = 50 \text{ MPa}$$

$$\sigma_{max} = \sigma_{ort} + R$$

$$= 20 + 50$$

$$= 70 \text{ MPa}$$

Soru-4)(20p.) Şekildeki gibi bir kiriş sistemine iki tane kuvvet etki etmektedir. Kirişin D noktasına gelen mesnet kuvveti nedir (N)? ($L_1=400 \text{ cm}$, $L_2=300 \text{ cm}$, $F_1=1000 \text{ N}$, $F_2=500 \text{ N}$)
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$$\sum M_A = 0$$

$$F_1 \cdot L_1 + F_2 \cdot (2 \cdot L_1) - R_{Dy} \cdot L_1 = 0$$

$$1000 \text{ N} \cdot 400 \text{ cm} + 500 \cdot 2 \cdot 400 \text{ cm} - R_{Dy} \cdot 400 \text{ cm} = 0$$

$$R_{Dy} = \frac{800000 \text{ Ncm}}{400 \text{ cm}} = 2000 \text{ N}$$